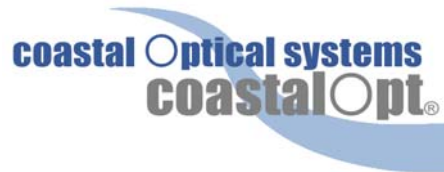


# Measuring surface slope errors on precision aspheres



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When is it important for an optical designer to control slope errors?  
(what types of optical systems?)

Laser radar transmitters that project laser beams into far field  
rely on a tight point spread function

High Energy Laser Systems that focus the energy into as  
small a spot as possible at the highest possible fluence

UV systems where mid-spatial frequency errors (ripple)  
degrade image quality

Grazing incidence optics

How should you specify surface slope error?

ISO 10110 is silent about how to quantify or measure surface slope errors

*ISO 10110 Part 5 has 25 pages on surface form tolerances and part 12 has 10 pages on defining aspheric surfaces, but neither mentions how to define a surface slope tolerance*

What units should be used to specify slope error?

Waves per cm?

Waves per inch?

Radians? Milliradians? Microradians?

Degrees?

# Example 1 - Laser dimensional gauging instrument

*ultra-LM like*

SURF.	RADIUS	TOL.	T. P. FIT (if reqd.)	IRREG (if reqd.)	SCRATCH AND DIG	CLEAR APERTURE	UNLESS OTHERWISE SPECIFIED
R <sub>1</sub>	1162±1.0	±0.02	NOTE	NOTE	SEE NOTE	6X130	DIMENSIONS ARE IN MILLIMETERS
R <sub>2</sub>							MINIMUM PROTECTIVE BEVEL ON ALL EDGES AND CORNERS
R <sub>3</sub>							WEDGE PYRAMID
R <sub>4</sub>							SCRATCH AND DIG PER MIL-Q-135X

REV.	RELEASE/RCN NO.	DATE
C	DE-0165	5-8
F	SCV-1077	11-21-77
G	ECN-1158	1-17-80
H	ECN-5527	11-23-87
J	ECN5850	1-18-89
K	ECO-0028	12-8-91

10. EXTERNAL FINISH FINEGRIND OR SAWCUT U.O.S.  
 9. APPLY STRIP-LAC TO OPTICAL SURFACE FOR PROTECTION AFTER Q.I.C. PROCESS.  
 8. SCRATCH + DIG 40-20 AND FIG. TOL. TO BE 7/10 CM, NO MK IX SLOPE TESTING.  
 7. TEST WAVEFRONT PER ATP-0097.  
 6. REFLECTIVITY TO BE UNIFORM ACROSS CLEAR APERTURE WITHIN 5% TOTAL.  
 5. CUT CENTRAL PORTION OF PARENT PARABOLA TO 15±1MM WIDE AND SAVE FOR MANUFACTURER OF 7030-1007 MIRROR.  
 4. NO SURFACE DEFECTS GREATER THAN 10µ IN WIDTH.

3. COATING TO BESS DURABILITY OF MIL-M-13508 WITH 100% INSPECTION FOR HARDNESS.  
 2. REFLECTED WAVEFRONT λ/15/CM OR BETTER OVER 6X120 APERTURE AND λ/2/CM OR BETTER OVER 6X130 APERTURE.  
 LOCAL LENGTH = 581±2MM

1/4 COMMERCIAL POLISH

220±1.0 CT AT VERTEX

150±0.2

160.0±0.5 DIA.

55.0±1.0

12.5 TO Q OF CLEAR APERTURE

R2

R1

OPTICAL AXIS

SQUARE TO OPTICAL AXIS WITHIN 0°0'30" (0.1 MM MAX EDGE RUNOUT REF)

MILLIMETER	INCH
15±1	.590±0.040
130	.5118
6	.236
1162	.4575
581±2	.2287±0.08
22.0±1.0	.866±0.040
0.1	0.004
160.0±0.5	6.30±0.02
12.5	.492
55.0±1.0	2.17±0.040
15.0±0.2	.591±0.008

CONVERSIONS

APPLICATION	QTY	USED ON	QTY
7030-0110	1	130E TRANS.	1

GLASS TYPE	MATERIAL	n <sub>d</sub>	TOL.	n <sub>e</sub>	R <sub>1</sub>	R <sub>2</sub>	R <sub>3</sub>	R <sub>4</sub>
PARABOLA SEGMENT	G33	1.5113	±0.0001	1.5113	1162			

OTHER: BIRKING INDEXTRE 56NM/CM λ(589)

MELT VARIATIONS (DO) (DO NOT) REQUIRE RECOMPUTATION

TITLE: PARABOLA SEGMENT

DESIGNER: T.J.D. DATE: 11-27-77 APPROVED: DATE: 11-30-79

CHECKED: DATE: APPROVED: DATE:

SCALE: 1/2 SHEET 1 OF 1

**-01CONF. 2 REFLECTED WAVEFRONT λ/15/CM OR BETTER OVER 6X120 APERTURE AND λ/2/CM OR BETTER OVER 6X130 APERTURE.**

## Examples #2

### Satellite instrument mirrors

#### 85 x 75 mm off-axis aspheric (oblate spheroid) mirror

**3.3.3 Surface Figure:** Surface 1 shall have a surface figure error of  $\leq 0.1\lambda$  rms over the entire clear aperture measured at or converted to 632.8nm. Surface slope errors shall be  $\leq 5 \text{ E } -5$  radians over the entire clear aperture.

#### 180 mm diameter parabolic mirror

**3.3.3 Surface Figure:** Surface 1 of [REDACTED] shall have a surface figure error of  $\leq 0.05\lambda$  rms measured at or converted to 632.8nm over the entire clear aperture as noted on **Sheet 3**. [REDACTED] (5000000000), and [REDACTED] shall have a surface figure error of  $\leq 0.05\lambda$  rms measured at or converted to 632.8nm over the entire clear aperture as noted on **Sheets 4**. Surface slope errors for all mirrors shall be  $\leq 5 \text{ E } -5$  radians over the entire clear aperture.

No indication of the spatial frequencies of interest

## Example #3 - COSTAR optical prescription

Table IV. Anamorphic asphere requirements

Acronym	d01	d06	d02	d07
AHRS	1.173965 E-3 ±.25%	1.0330 - 1.0340	3.2470 E-7 ±1.0%	1.0395 - 1.0415
AFOS	1.660584 E-3 ±.25%	1.1310 - 1.1330	9.7435 E-7 ±1.0%	1.2330 - 1.2360
AFOC	1.709724 E-3 ±.25%	1.00265 - 1.00285	9.7845 E-7 ±1.0%	1.004 - 1.006

Acronym	Surface Figure	Surface Roughness RMS
AHRS	$\lambda/100$ RMS	$< 10 \text{ \AA}$
AFOS	$\lambda/100$ RMS	$< 10 \text{ \AA}$
AFOC	$\lambda/100$ RMS	$< 10 \text{ \AA}$

14-18 mm aperture

Notes:

$Z = d01 (d06 X^2 + Y^2) + d02 (d07 X^2 + Y^2)^2$  ACCOS V Format  
 All optics are concave  
 $\lambda = .6328 \text{ mm}$   
 All surface errors are RMS waves

Surface Error Bandwidths

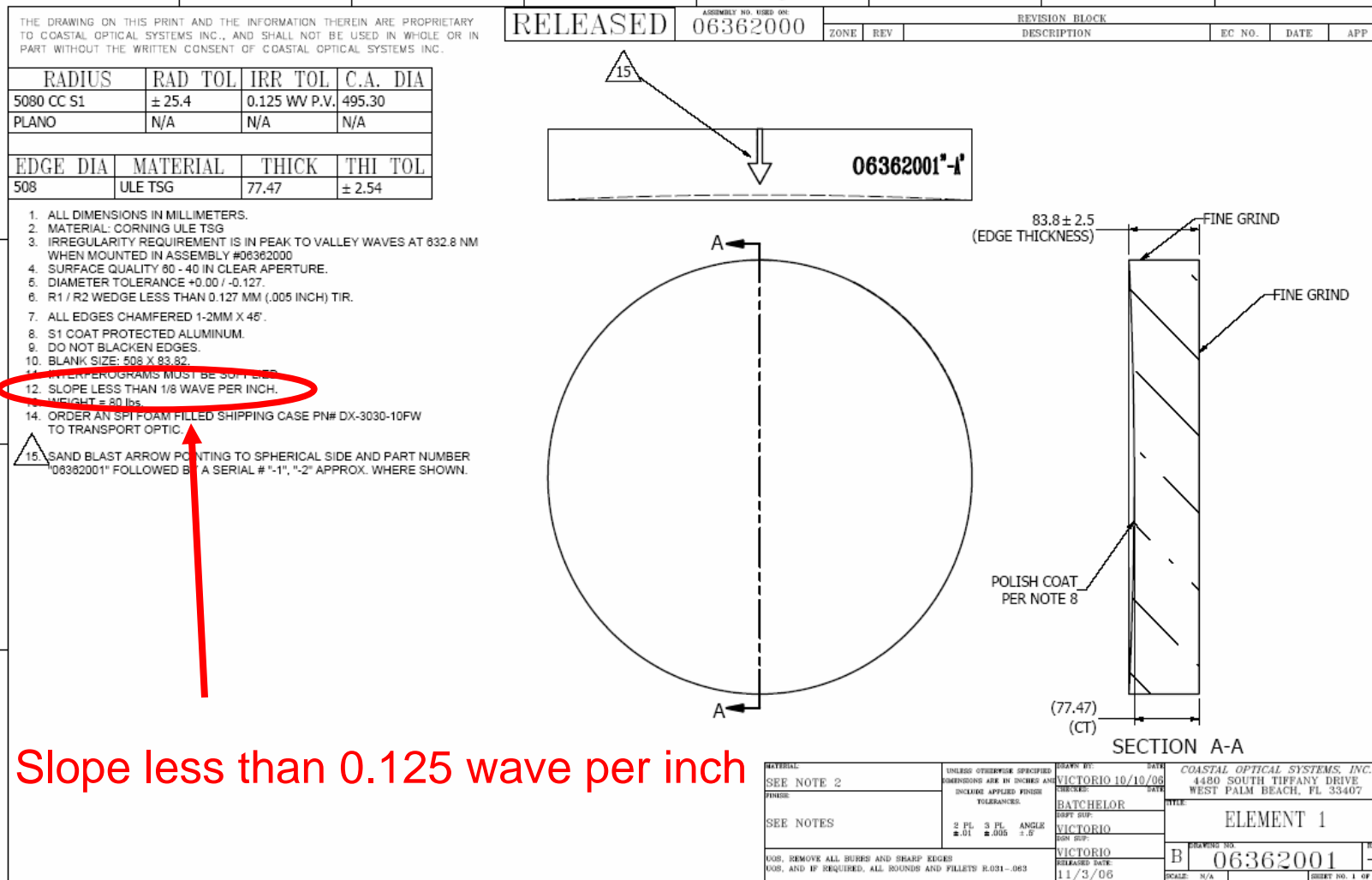
Surface Errors

Spatial Frequencies

Surface Figure  
 Surface Roughness

$> 1 \text{ mm}$   
 $< 1 \text{ mm}$

## Example #4 - 0.5 meter (20 inch) diameter mirror



## Example #5 - NIF Small Optics

Drawings control form, figure, rms slope, sampling and filtering<sup>1</sup>

Lambda/8 peak to valley

Lambda/40 rms

Lambda/30/cm RMS gradient

With these values evaluated for spatial periods greater than 2 mm only.

All interferometry must have a minimum of 200 pixels across the aperture

“Surface Figure and Roughness tolerances for NIF optics and the interpretation of the gradient, P-V wavefront and RMS specification”, Lawson, Aikens, English, Whistler, House and Nichols, UCRL-JC-134534 presented in Denver, CO, July 1999

## NIF small optics drawings also explicitly specify the filtering that should be used when using interferometers to evaluate surfaces

The wavefront error for individual optics is derived from the error budget permitted for the laser beam using system models. Specification for surface form as well as transmitted and reflected wavefront errors are applied. In particular, the RMS gradient of the wavefront error (RMS Gradient) is specified because it has the best correlation with the focusability of the beam. Because of the relationship between the spatial frequency of a given error and its effect on laser system performance, spatial filtering is applied (>2 mm). **This approach is outside the framework of ISO 10110.** Clarifications are provided where necessary. In addition, the surface form and wavefront specifications apply after coating in the use environment.

## What metrology tools are used to measure surface slope of optics?

Instrument	Comments	Examples of commercial instruments
Contact profilometers	Profilometers typically measure surface topography (sag) and do not report slope	Taylor Hobson, Mititoyo and others
Shack Hartmann sensors	Wavefront sensors determine wavefront error through slope measurement	Wavefront Sciences and others
Phase measuring microscopes	Measure phase like a Fizeau interferometer, do not measure slope directly	Zygo New View 5000, ADE Phase Shift and others
Polarized topology optical scanning profilometers	Measure slope directly	Chapman Instruments
Fizeau Interferometers	Calculate slope from phase data	Zygo, ADE, 4D and others

## How does an interferometer calculate slope?

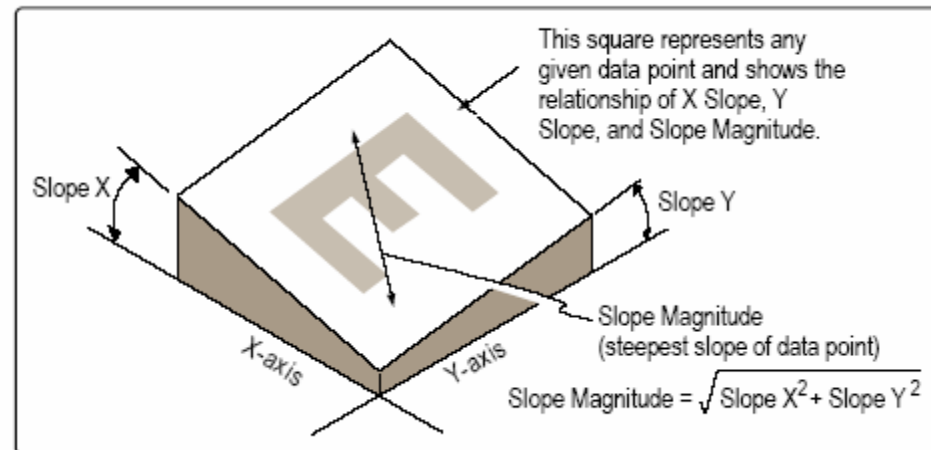
For Data Point E:

$$\text{Slope X} = \frac{F - D}{2}$$

$$\text{Slope Y} = \frac{B - H}{2}$$

A	B	C
D	<b>E</b>	F
G	H	I

This block represents any given group of nine adjacent data points.



From MetroPro Reference Guide OMP-0347J (figures used with permission)

Why is slope difficult to measure on aspheres?

Pupil focus problems on non-null cavities

Surface defects influence measurements on high-resolution interferometers

Environmental effects from long cavity lengths

Tilted apertures & surfaces under test

Slope measurements (like figure measurements) are **strongly dependent** on spatial sampling & filtering

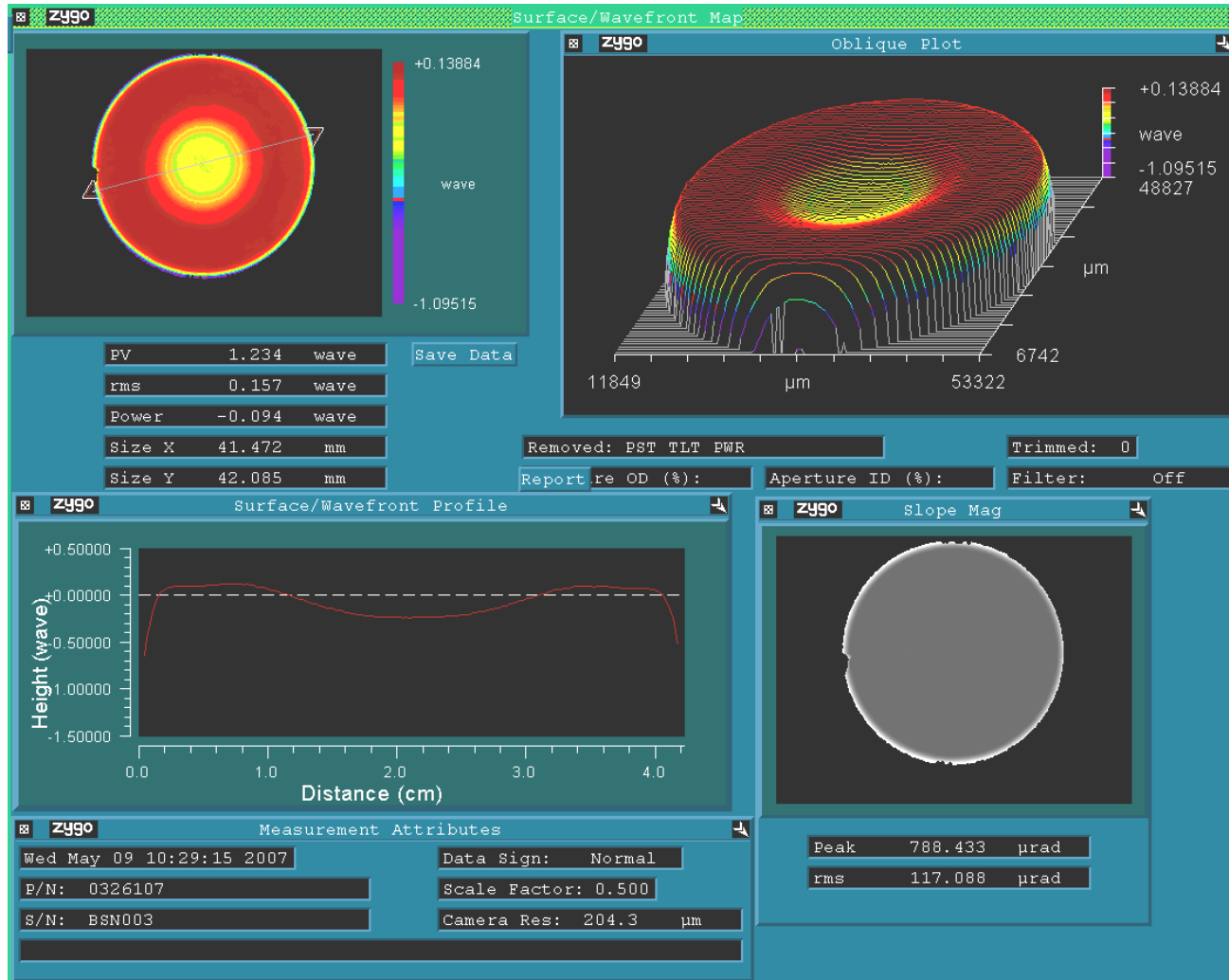
## Influence of pupil focus on non-null cavities



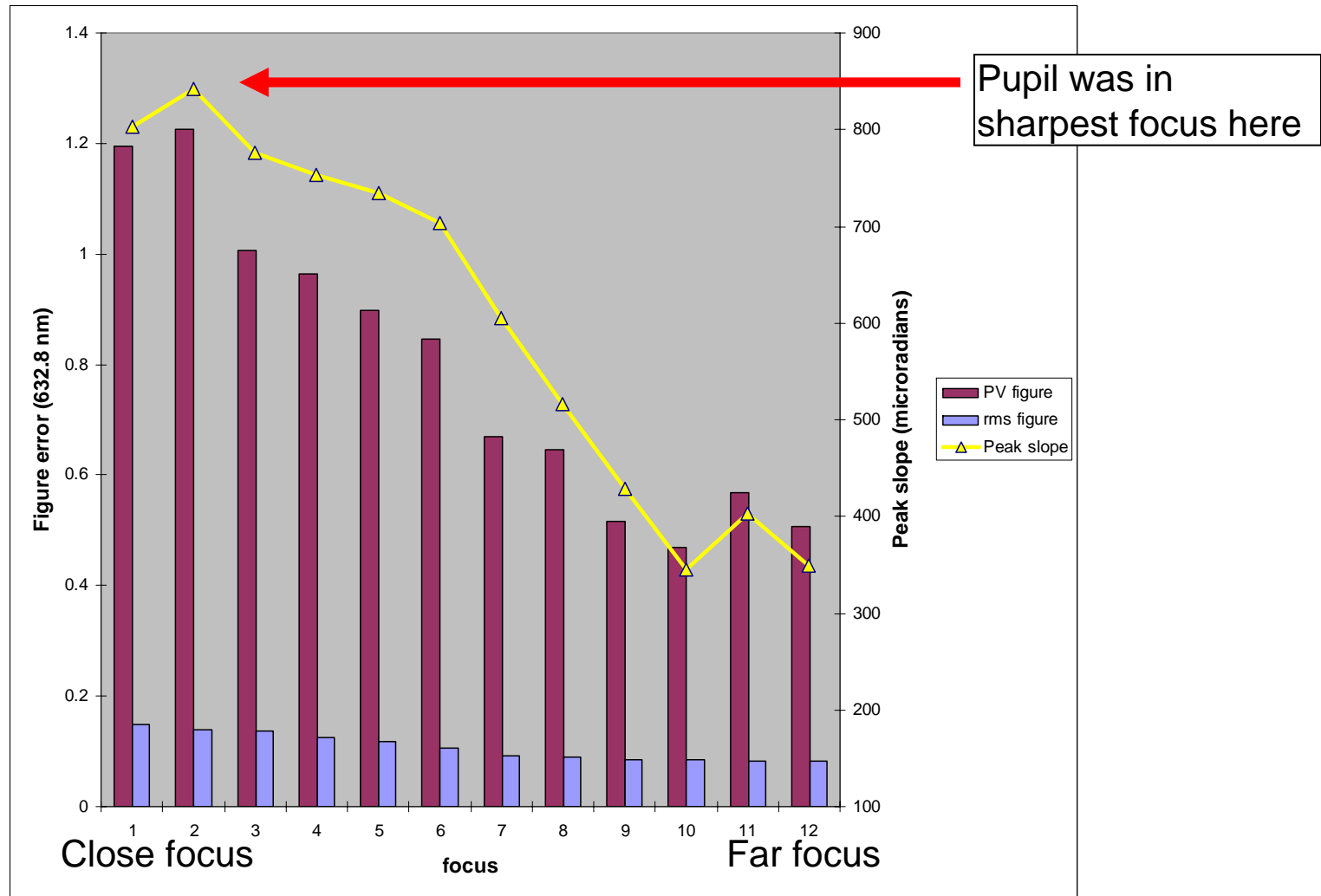
- f/3.3 focal ratio
- 3 phase averages
- No trim
- No filters
- 42 mm diameter

*See Lowman and Greivenkamp "Modeling an interferometer for non-null testing of aspheres" SPIE 2536, p. 139 for mathematical model of the influence of aberrations of the pupil and definition of the pupil on test results*

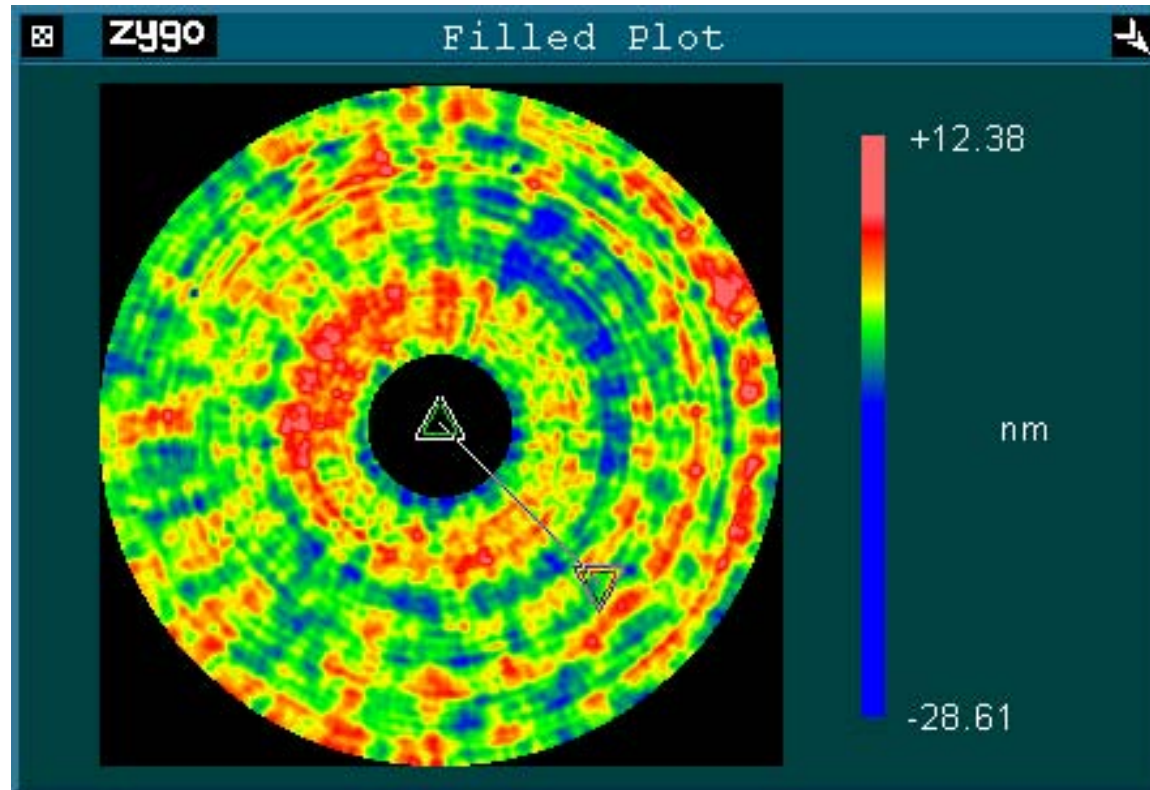
Extreme edge of surface has (real) zone of high slope (roll-off)



## Figure Error and Peak Slope error as a function of pupil focus



## Surface Defects influence slope on high resolution interferometers

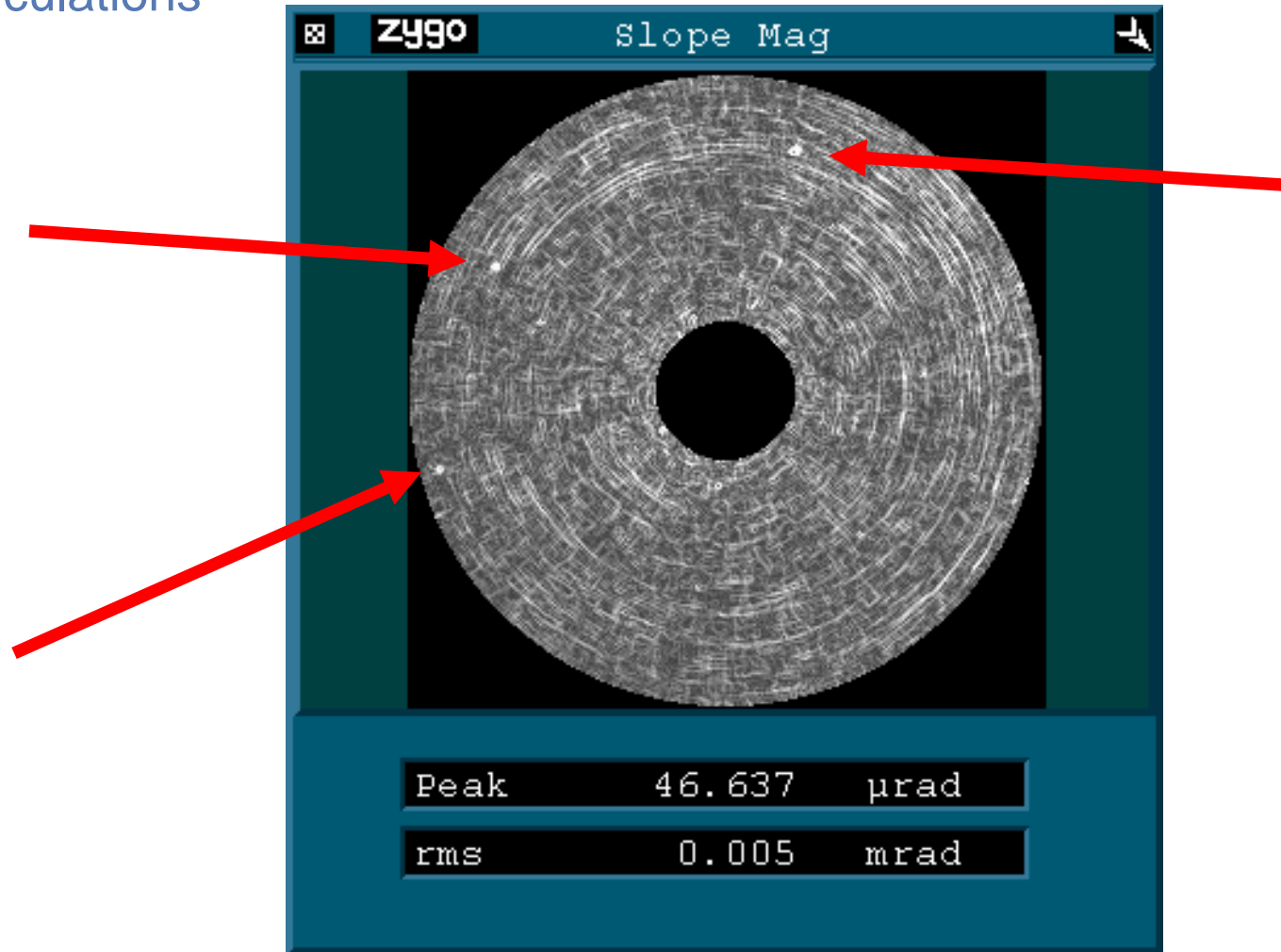


95 mm diameter convex parabolic mirror

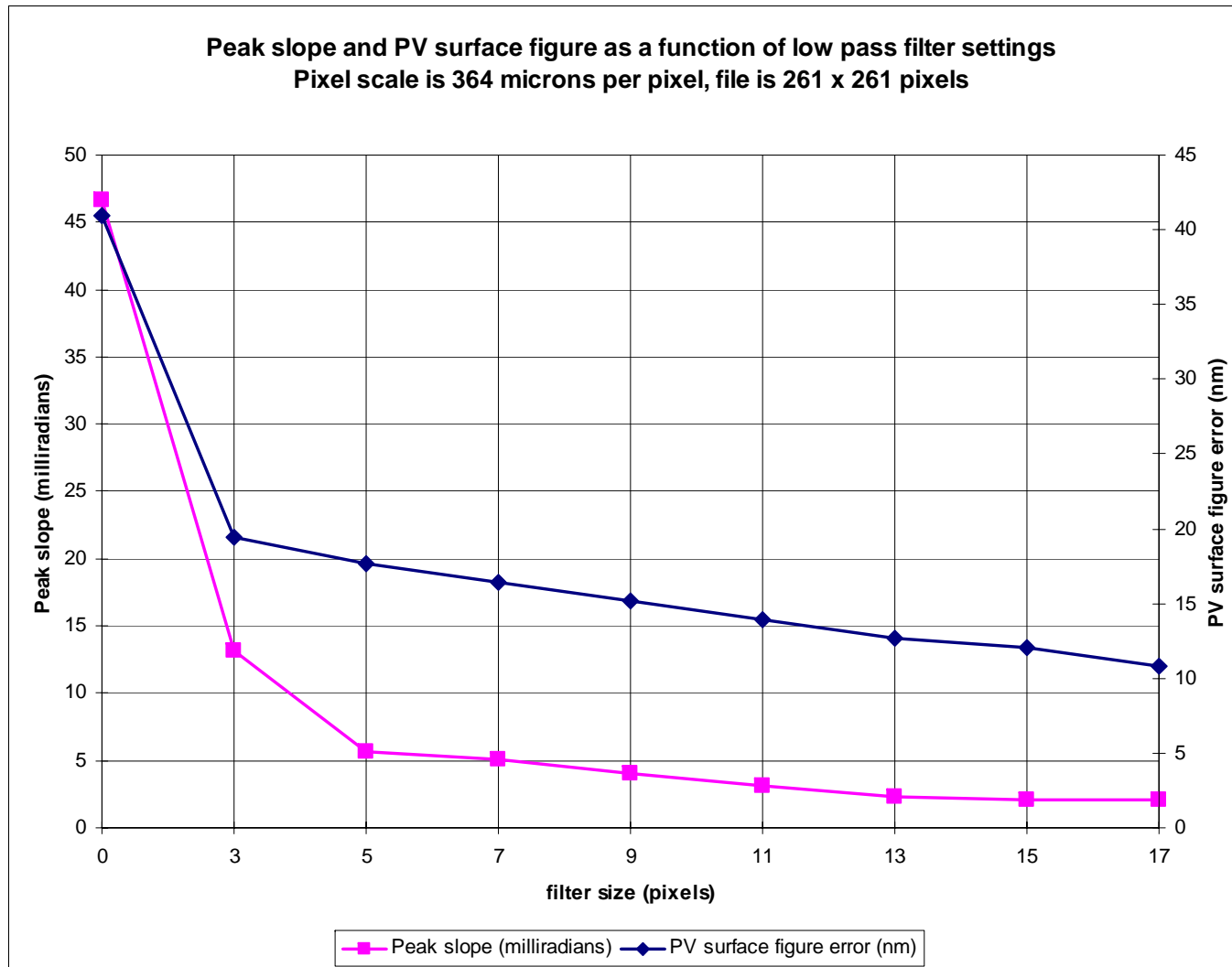
Measured on SSI-A with 1k x 1k camera

0.0647 wave peak to valley, 0.006 wave rms

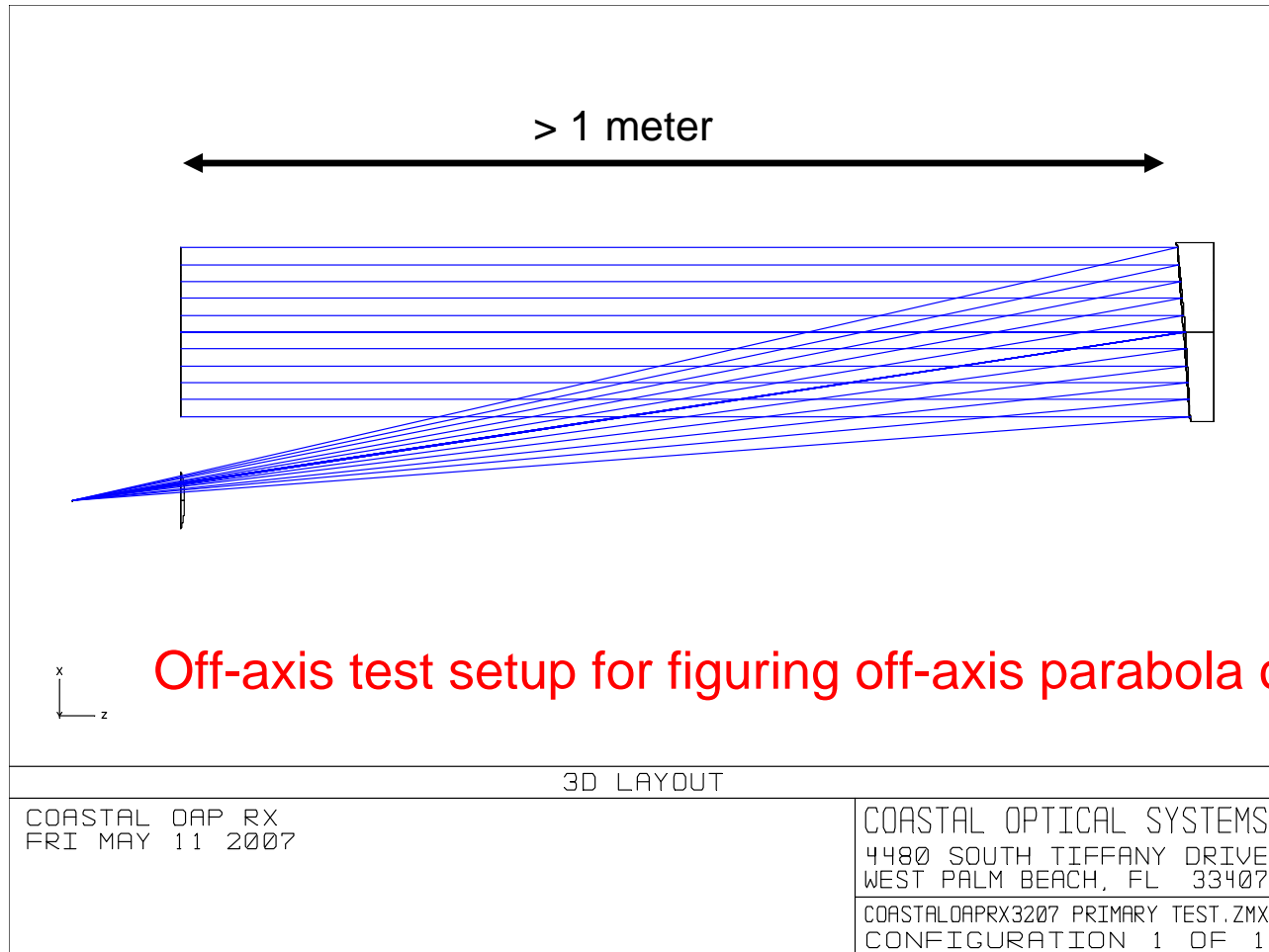
# Surface defects or contamination on surface under test influence slope calculations



## Using filtering to get any answer you want



## Long cavities and tilted stops cause false focusing and field curvature



*For further explanation, see Schillke, "Critical Aspects on testing aspheres in interferometric setups"*

## Example of insufficient spatial sampling – convex parabolic mirror

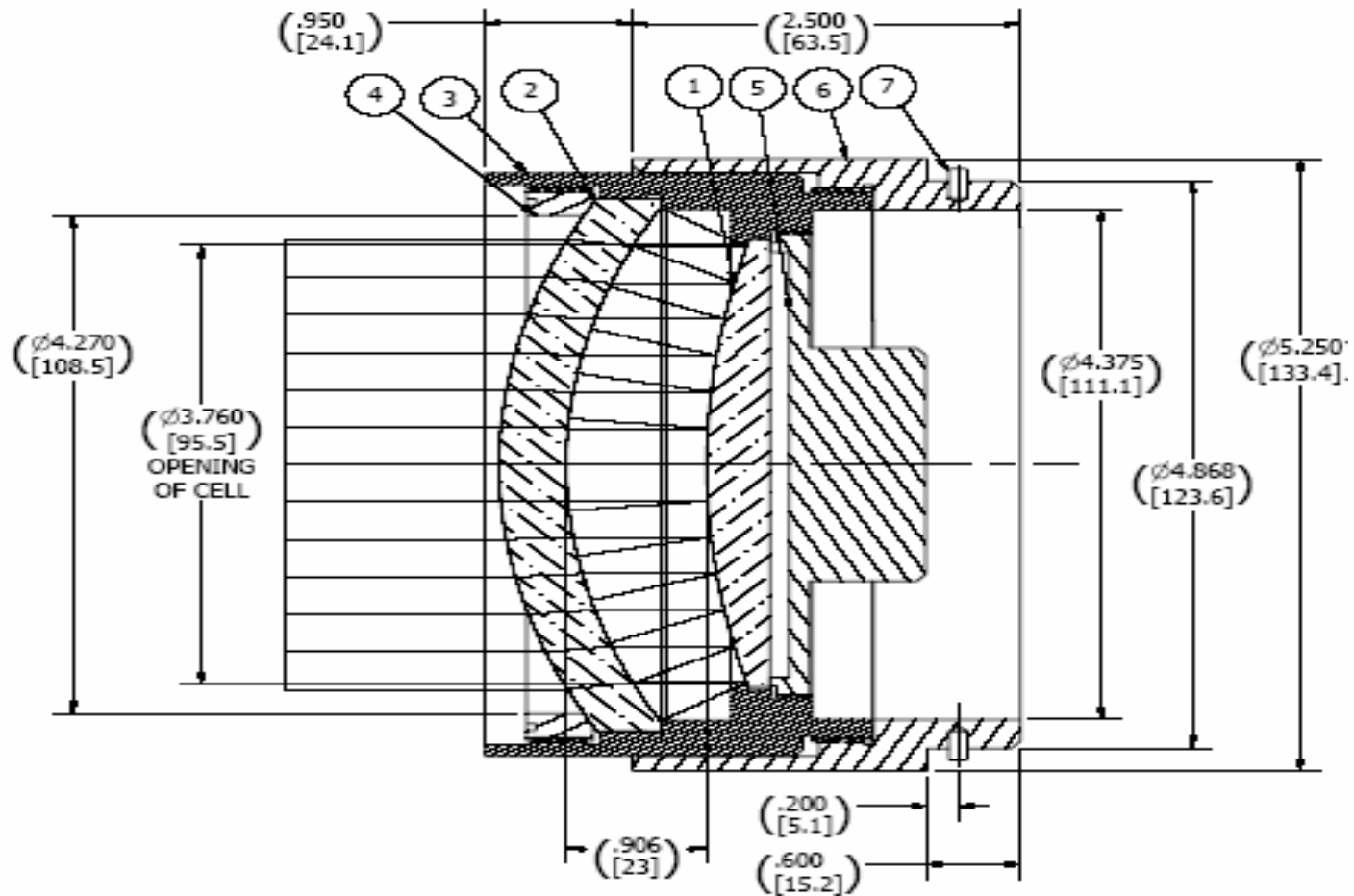
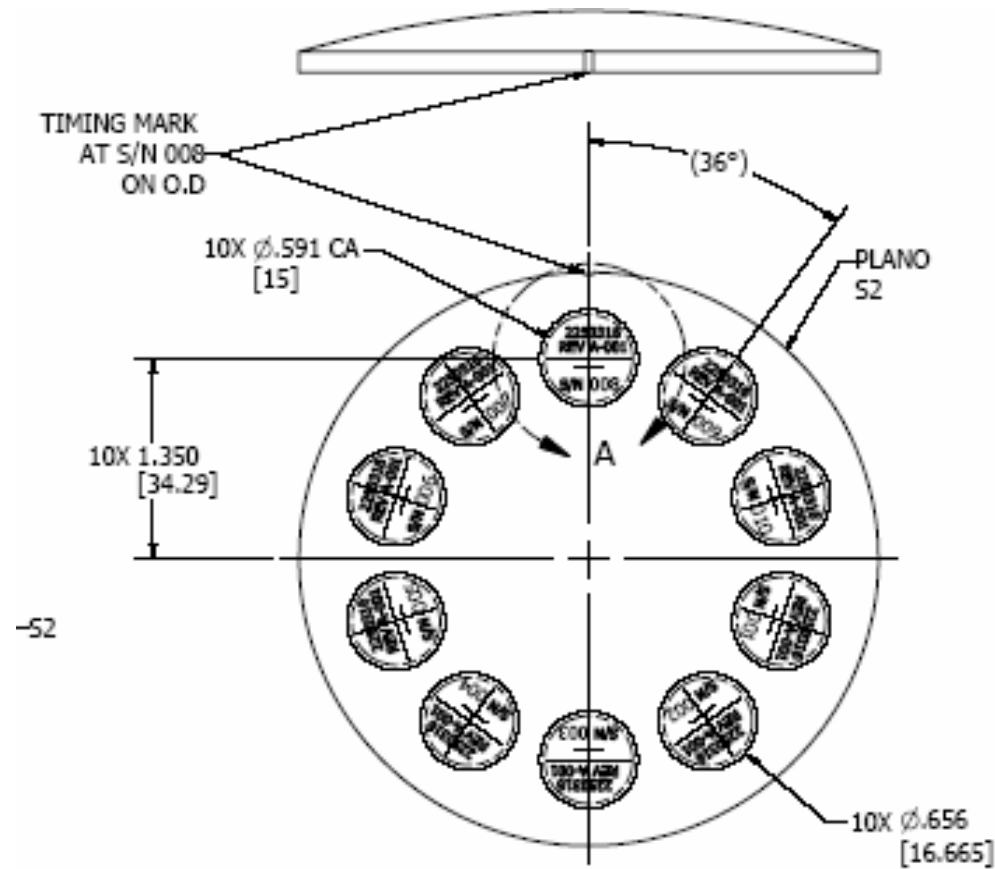
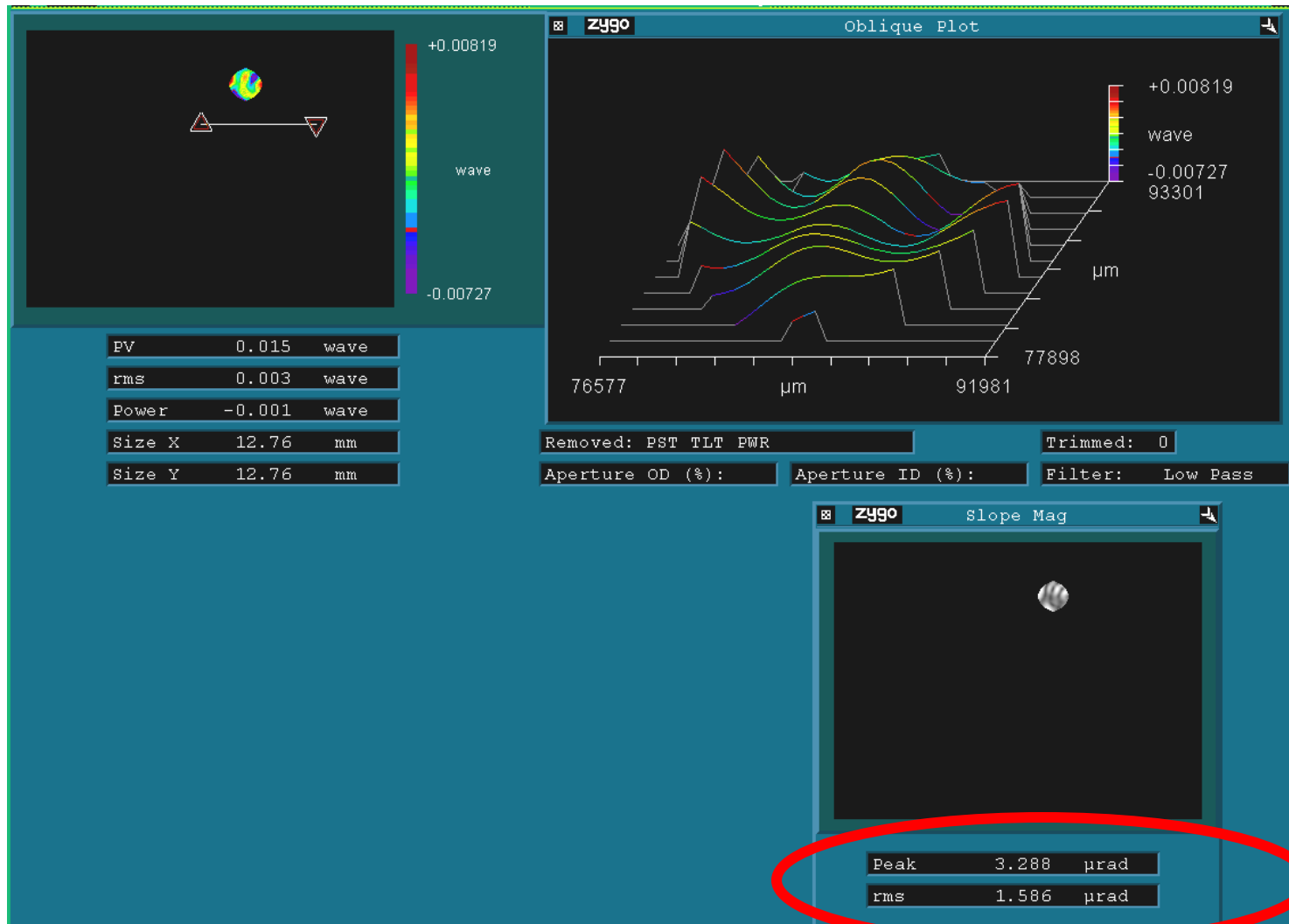


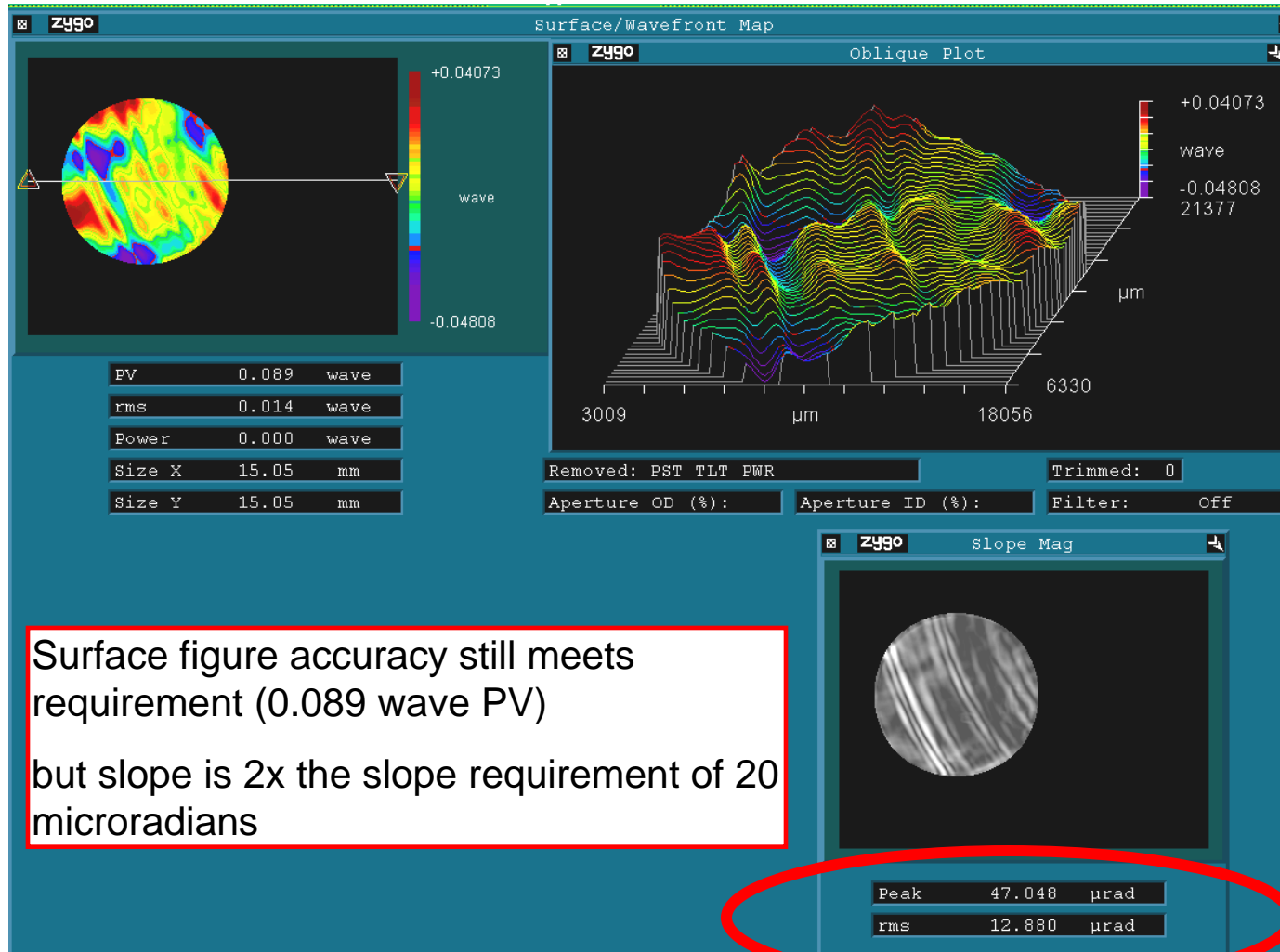
Figure and slope was tested moving cursors around parent



Sub-apertures were tested by moving software mask around the parent to the different locations

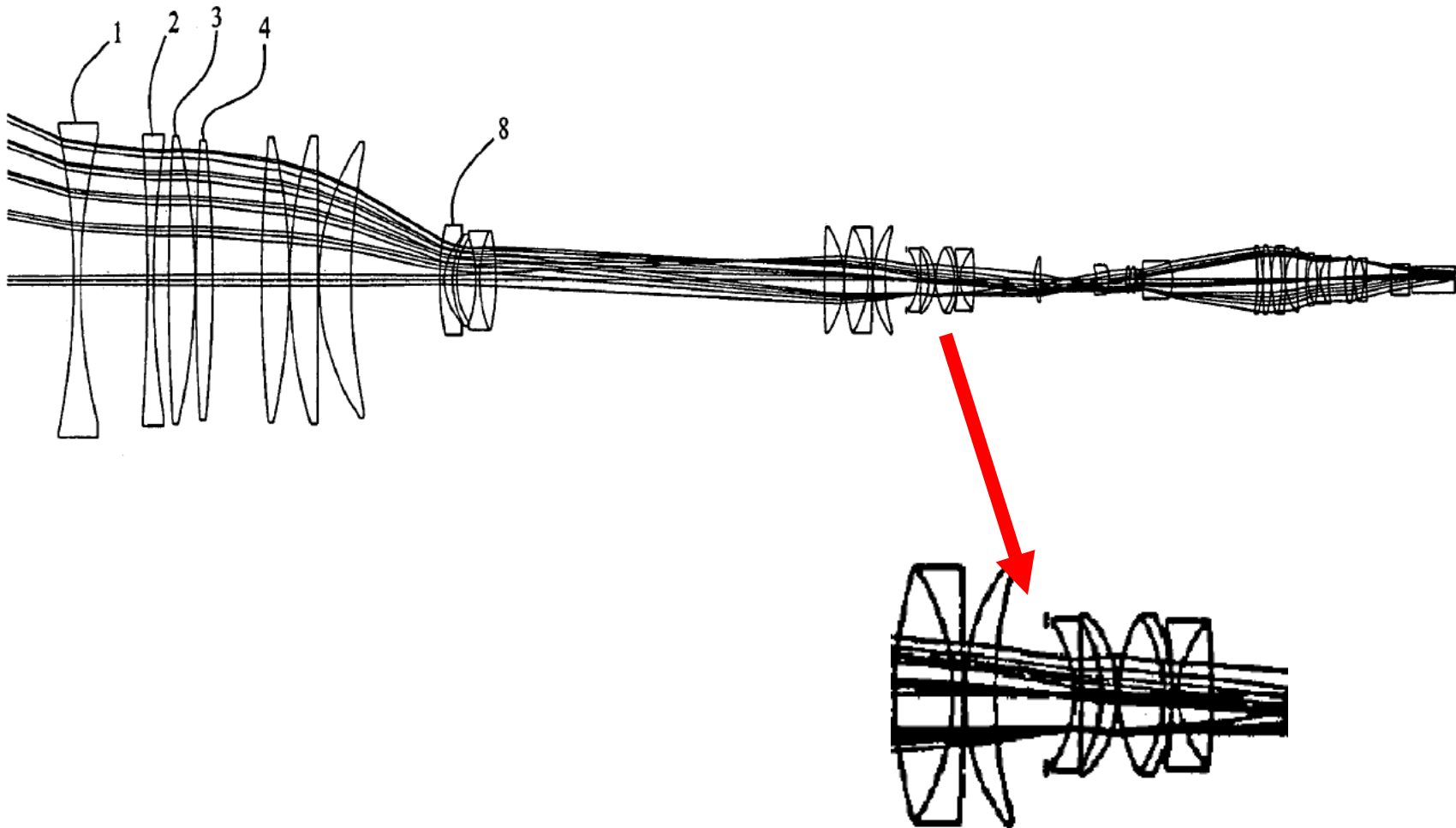


When tested individually, the off-axis segments showed slope error

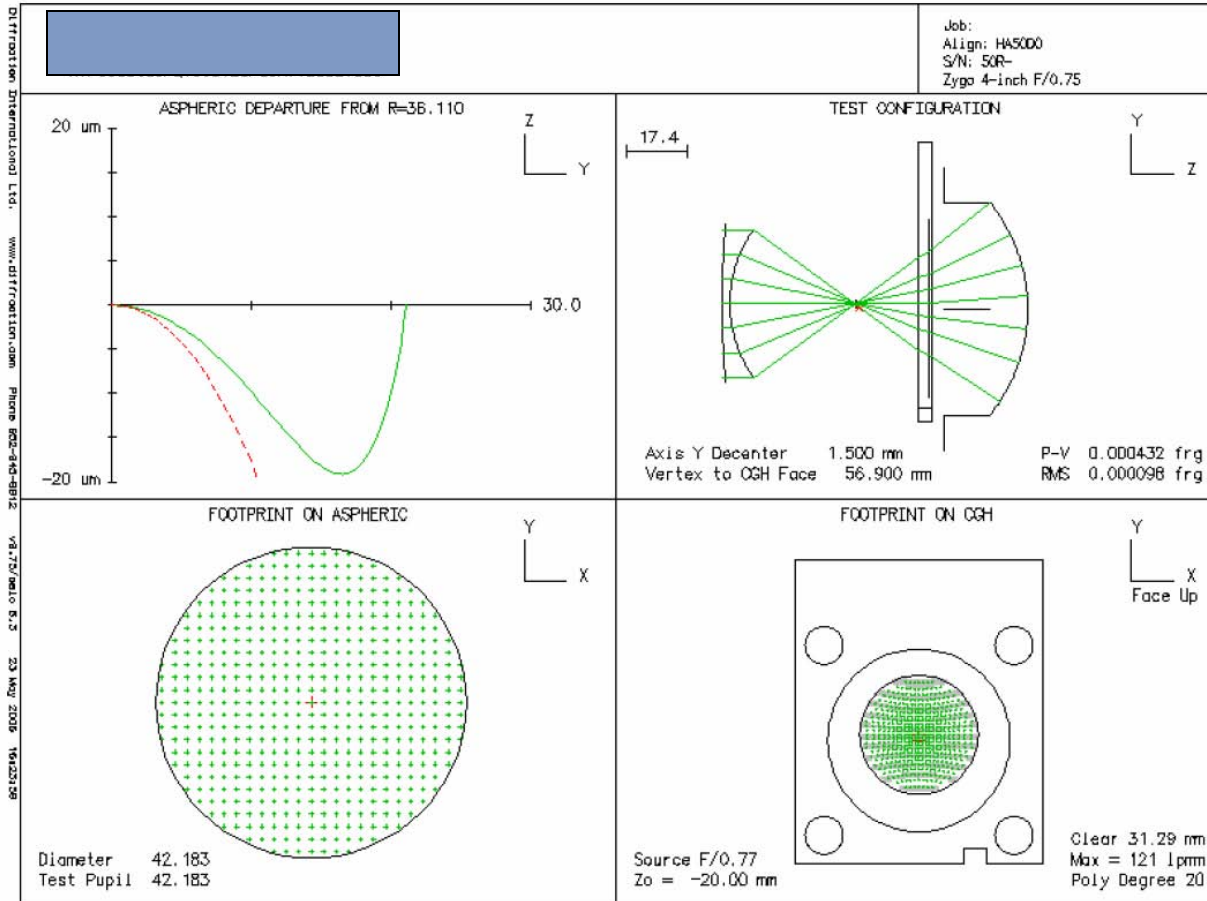


Surface figure accuracy still meets requirement (0.089 wave PV)  
but slope is 2x the slope requirement of 20 microradians

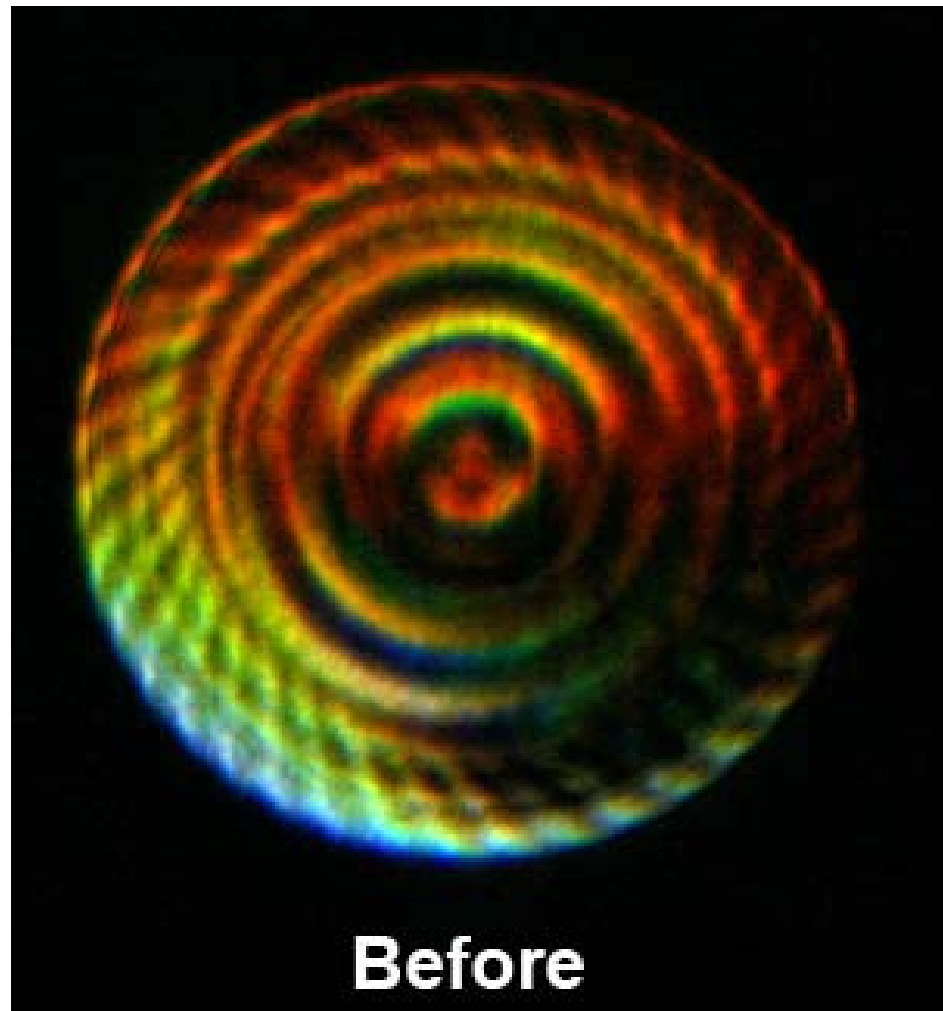
## Large zoom system example



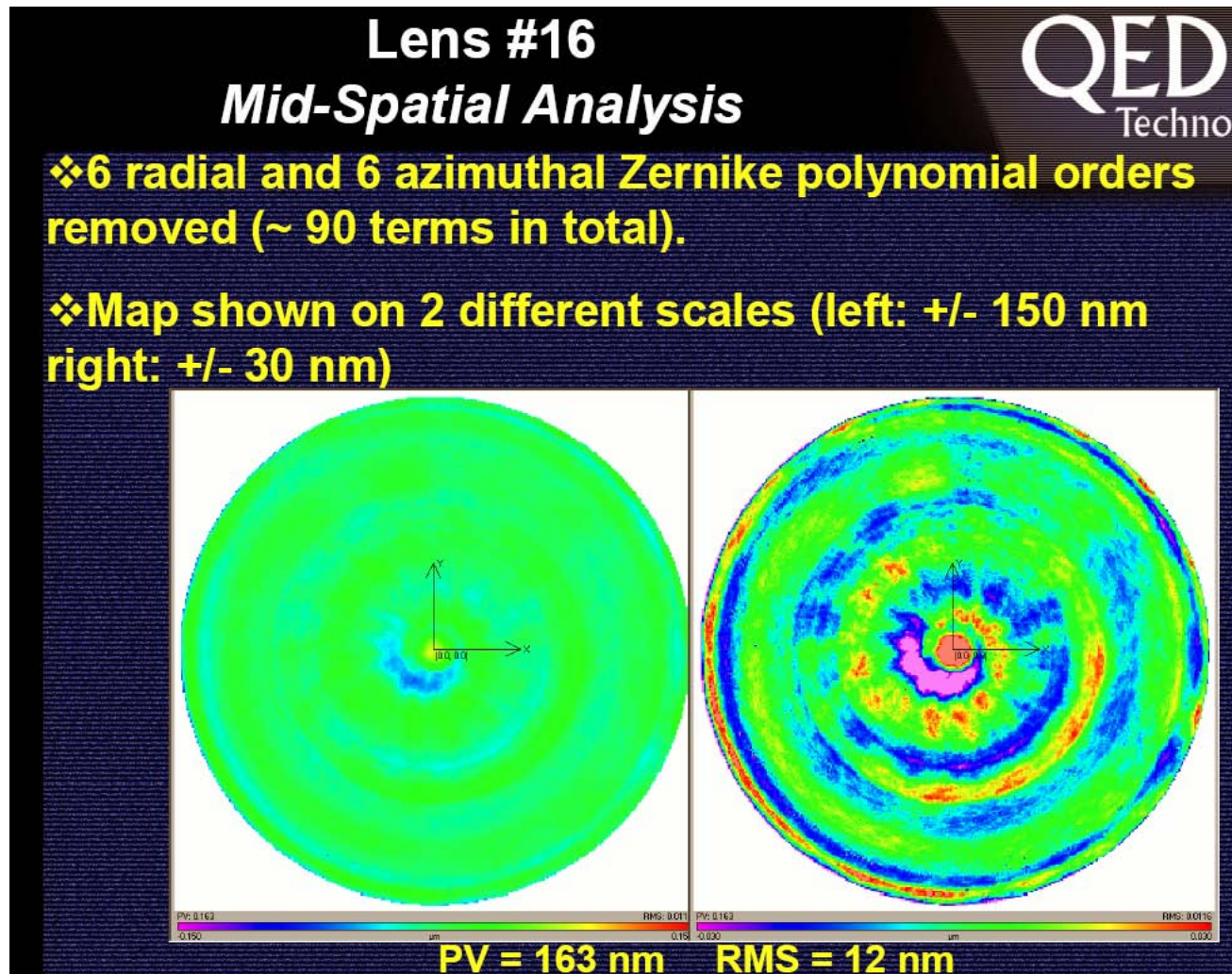
Higher order asphere R(best fit) = 36.11mm, 42 mm dia.



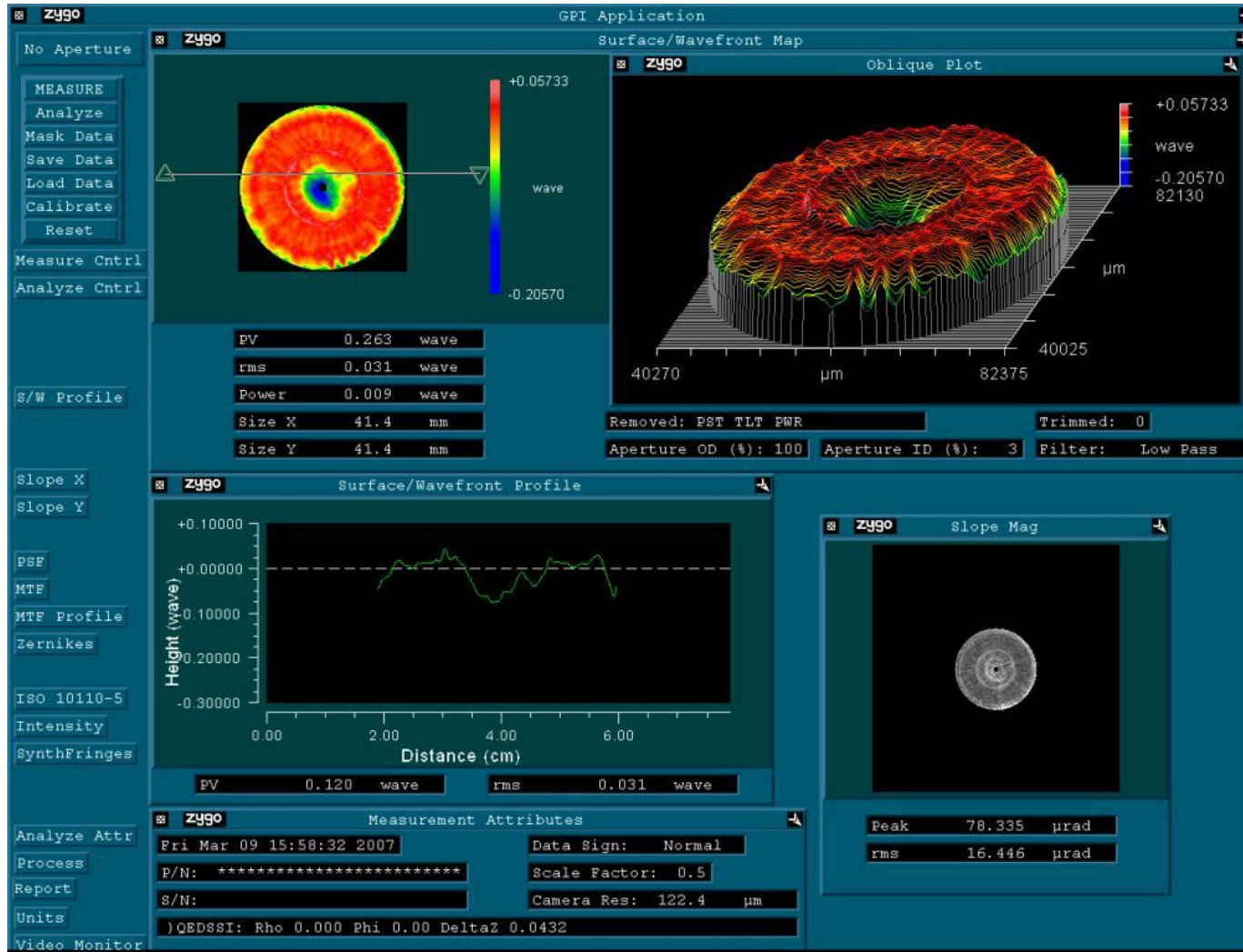
## Knife-edge test through as-built system



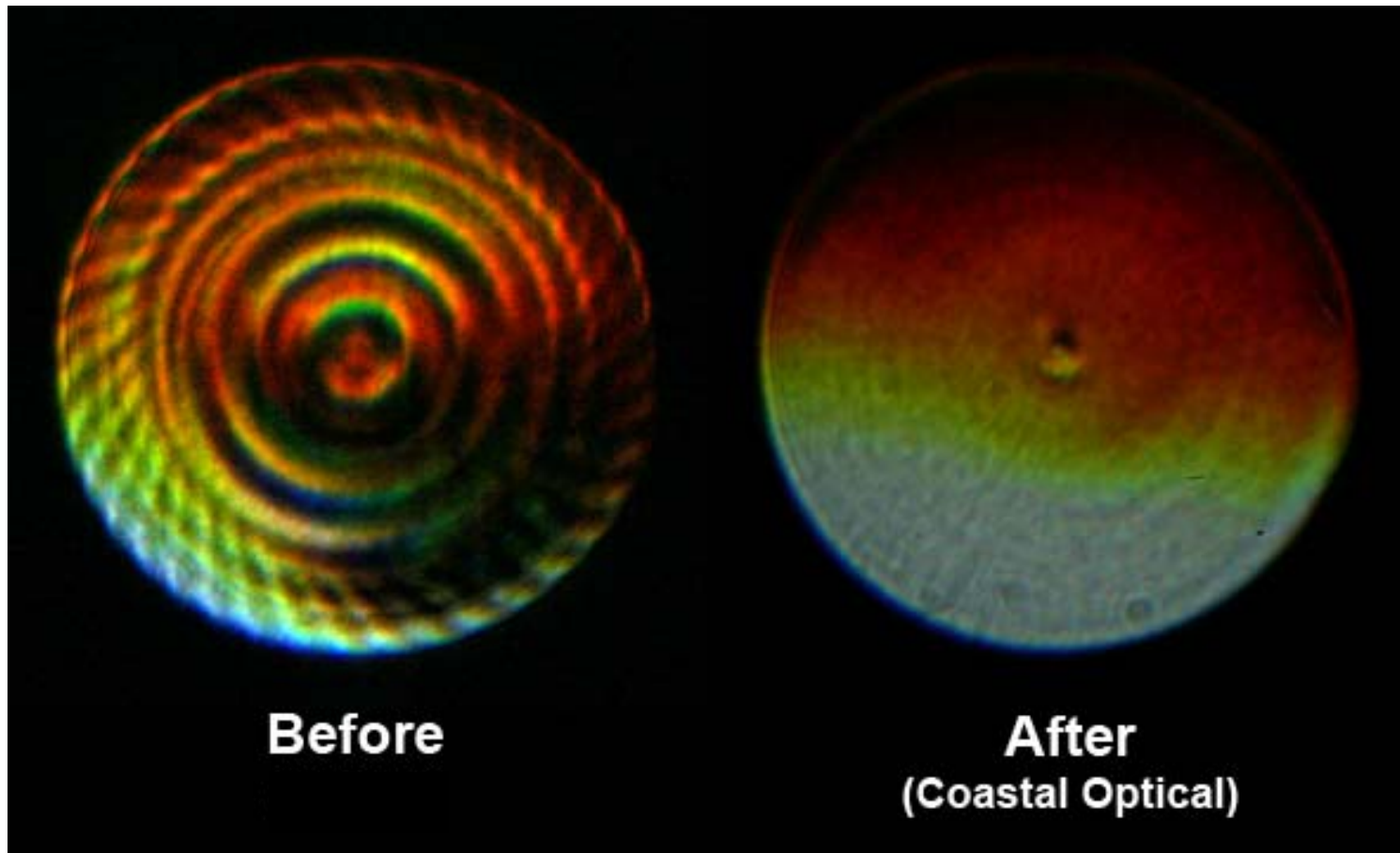
Testing on SSI showed zonal errors under lower order aberrations



# Replacement aspheres polished with MRF and tested with SSI-A



## Before and after system knife edge (Foucault) test



## Concluding thoughts and guidelines

The optical designer should define what spatial frequencies must be captured when specifying slope requirements.

The metrologist can then make sure that they have sufficient interferometric pixel sampling to cover the spatial frequencies of interest

You can not scale slope measurement. If a part measures 0.25 wave per cm, that does not mean you can say the part is 0.635 wave per inch.

If trying to get accurate slope measurements:

Zoom up the pupil image to use the most pixels in the aperture

Always use 4" to 33mm aperture converter for small pupils

Use care when focusing the pupil

For aspheres, you should have 200+ pixels across the aperture because there may be mid-spatial frequency errors

Powerful analysis tools like sampling and filtering options will often distort the slope results. *Filter with caution.*

## References

- “Surface Figure and Roughness Tolerances for NIF optics and the Interpretation of the Gradient, P-V Wavefront and RMS Specifications”*, Lawson, Aikens, English, Whistler, House and Nichols, LLNL UCRL-JC-134534 presented at Denver, CO July 18, 1999.
- “Slope Error Tolerances for Optical Surfaces”*, John R. Rogers, Optifab 2007.
- “Critical aspects on testing aspheres in interferometric setups”*, Frank Shillke, Carl Zeiss EUROPTO Conference on Optical Fabrication and Testing, Berlin, Germany, May 1999.
- “Modeling an interferometer for non-null testing of aspheres”*, Andrew Lowman and John Greivenkamp, SPIE Vol. 2536, p. 139-147.



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